

# Constraining the correlation distance in quantum measurements from the Moon

Version 10 May 2010

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- Reminder of Bell inequalities - The latest test
- Spatio-temporal dependance of correlations?
- Lunar and other tests

updates and developments at

<http://luth7.obspm.fr/~schneider/qm.html>

# Reminder: rules of Quantum Physics

**R0** An experiment can be divided into an apparatus and a system

**R1** Every system  $S$  is described by a Hilbert space  $Hilb$ .

$$\text{For } S = (S1, S2), \quad Hilb = Hilb1 \otimes Hilb2$$

**R2** A system can be in different states, described by  $\psi \in Hilb$

$$\text{For } S = (S1, S2), \quad \psi = \psi 1 \otimes \psi 2$$

**R3** A system usually evolves according to the equation  $-i \hbar d\psi/dt = H\psi$

State

**R4** Experiments lead to observables described by  $A \in Herm(Hilb)$

Observable

**R5** Only possible results of measurements of  $A$  are proper values  $a_i$   $A\psi_i = a_i\psi_i$

**R6** Results of measurements are random with probabilities  $p_i = |\langle \psi | \psi_i \rangle|^2$

**R7** After a measurement the system is in a state  $\psi_i$

# Comment on rules of Quantum Physics

- The mathematics of rules: no problem, universal consensus
- The rules also contain words from plain language:
  - « apparatus », « experiment », « measurement »,  
« observable », « result »

These common-language, unavoidable, words are the source of controversies in the understanding of quantum physics.

# A problem with quantum rules

Question: what is the meaning of superposed states?

Let  $|+/-x\rangle$  be the eigenstate of  $\sigma_x$  for the proper value  $+/-1/2$

$$|+/-x\rangle = (|+y\rangle +/- |-y\rangle) / \sqrt{2}$$

The measurement of  $\sigma_y$  gives  $+1/2$  or  $-1/2$  with probability 50%

==> Two possible views (or « interpretations »):

- 1/  $|+x\rangle$  « has » no definite value of  $\sigma_y$  prior to measurement (QM)
- 2/  $|+x\rangle$  « has » a definite value of  $\sigma_y$  but it is unknown.

A complete description of the state  $|+x\rangle$  then requires extra « hidden » parameters .

(similar e.g. to positions and velocities of individual molecules of a gaz with temperature  $T$  )

# A problem with quantum rules

Hidden parameters  $\lambda$  with distribution probability  $\rho(\lambda)$

$$|x\rangle \longrightarrow \blacktriangleright |x, \lambda\rangle$$

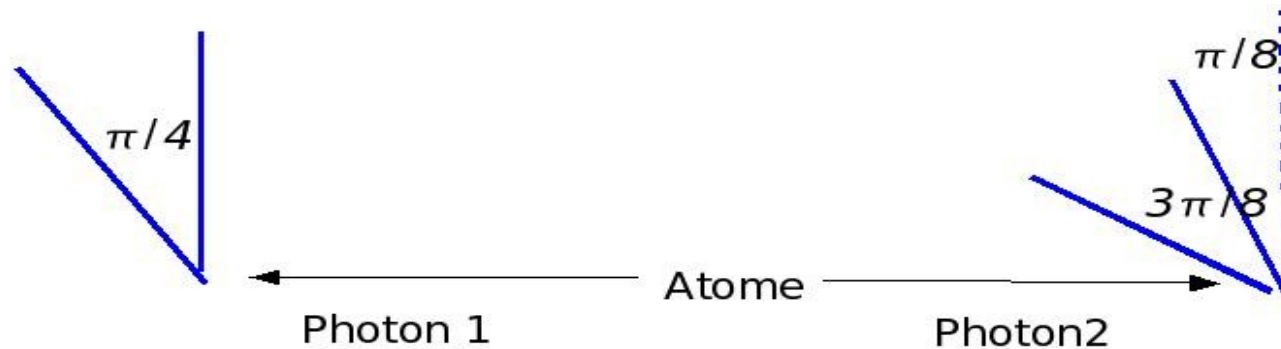
## Bell theorem

Consider then a 0 spin system decaying into 2 spin  $\frac{1}{2}$  systems  
1 and 2 (inspired by Einstein-Podolski-Rosen paradox EPR)

Conservation of spin  $\implies$  in any direction  $a$ ,

$$(\sigma_a)_2 = -(\sigma_a)_1$$

# Bell theorem (2)



4 statistical correlations:

$$C(0, \pi/8), C(0, 3\pi/8), C(\pi/4, \pi/8), C(\pi/4, 3\pi/8)$$

- Suppose  $\lambda$  attached to 1 and 2 (local hidden variables)

Prediction from local hidden (Bell theorem)

$$C(0, \pi/8) - C(0, 3\pi/8) + C(\pi/4, \pi/8) - C(\pi/4, 3\pi/8) < 2$$

**whatever**  $p(\lambda)$

- Prediction from standard MQ :

$$C(0, \pi/8) - C(0, 3\pi/8) + C(\pi/4, \pi/8) - C(\pi/4, 3\pi/8) = 2\sqrt{2}$$

# Bell theorem (3)

- Other possibility: non-local hidden parameters
- A physical model (Bohm, Vigier et al ~'60):
  - Waves are « real physical objects »
  - Quantum system made of/embedded in a « subquantum », chaotic, medium in which hidden parameters propagate at a speed  $\gg \gg c$ .
  - These hidden parameters behave as « effective » non local parameters
  - Then possible to reconcile these hidden parameters with prediction of standard QM

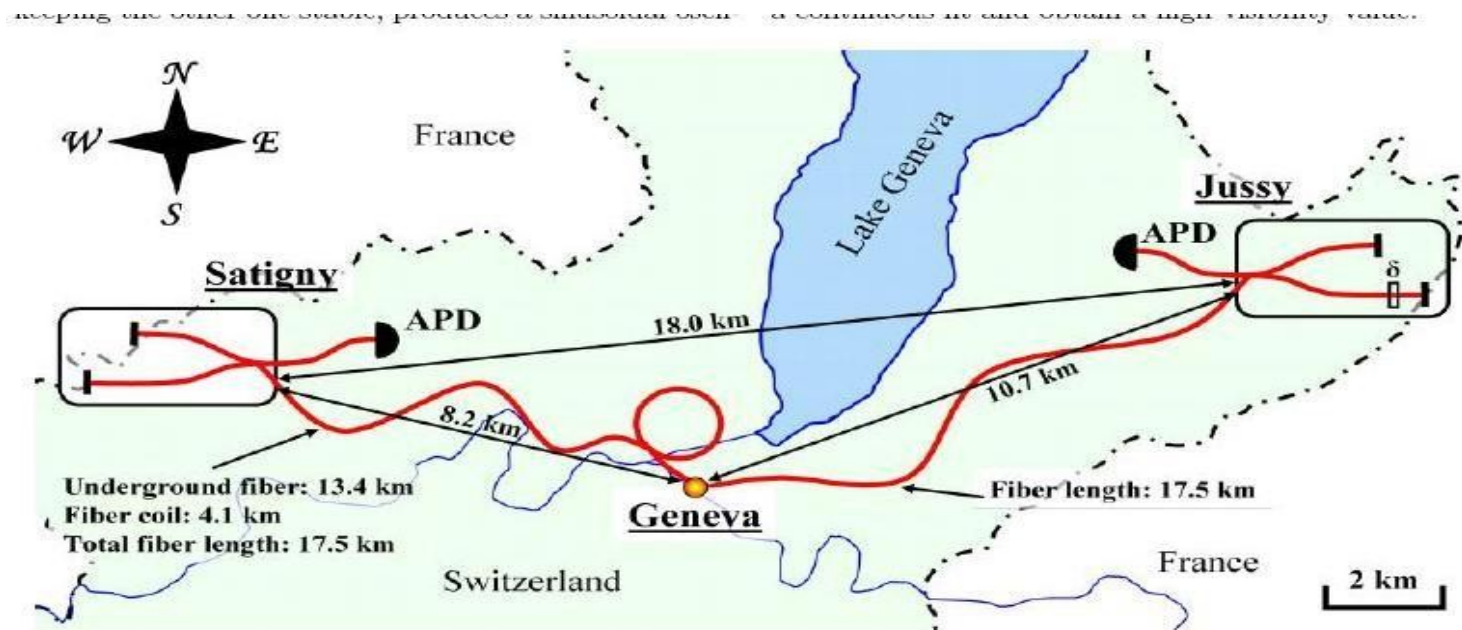
# Bell theorem (4)

- QM  $\implies$  Instantaneous statistical correlation at a distance **whatever the distance between detectors** (propagation speed  $V$  infinite)

- Experiment confirms prediction of standard QM

Tested until 18 km between 2 detectors ( $V > 10^7 c$ )

Gisin et al 2007





# Spatio-temporal dependance of correlations ? (1)

Questions:

- Does the correlation distance  $D$  go until infinity ?  
(even beyond the cosmological horizon ? )
- Is the « correlation speed »  $V$  necessarily infinite ?

Standard QM: **YES**

B.-V's or other theories answer: ??

4 possibilities:

- $D$  infinite,  $V$  infinite (standard QM)
- $D$  infinite,  $V$  finite (« dynamic correlation »)
- $D$  finite,  $V$  infinite (« static correlation »)
- $D$  finite,  $V$  finite (« dynamic correlation »)

# What distance $D_0$ and speed $V$ of correlation?

- Play only with  $G, h, c$

$$D = \sqrt{\frac{Gh}{c^3}} = 10^{-33} \text{ cm} \qquad V = c$$

- Play also with  $m_Q$  (quark mass, Higgs mass...)

$$D = \sqrt{\frac{Gh}{c^3}} \left( \frac{Gm_Q^2}{hc} \right)^N = 10^{-33-39N} \text{ cm} \qquad V = \left( \frac{Gm_Q^2}{hc} \right)^N c = 10^{-39N} c$$

- Play with non standard phenomena

- « 5th force »:  $D \sim 1 \text{ cm} - 1 \text{ m}$
- MOND (dark matter):  $D \sim 1 \text{ Mpc}$
- Cosmological constant  $D = 10 \text{ Gpc}$

Conclusion: no obvious prediction

# A test

Idea: measure  $D_o$  and  $V$

e.g.  $C(\theta, \theta', D) = C_o (D_o/D)^{-n}$       or       $C(\theta, \theta', D) = C_o (1 - e^{-D/D_o})$

(e.g. Introduce a dissipative term in Schröd. eq.:  $d\psi/dt = iH\psi + [\rho, H]$  )

==> Extend as much as possible the distance of measurement of correlations

e.g.: **Earth-Moon distance** (18 km ---> 400.000 km)

==> Put the (orientable) polarizers and detectors on the Moon

Put the laser source on the Earth and point it toward the Moon..

Remark: influence of gravitational waves background negligible  
(Raynaud, Lamine et al. GRG 36, 2271, 2004)

# A fundamental question

Suppose mirror on the Moon and detectors on Earth  
Easier to do than to put detectors and tunable polarizers on the Moon

MQ: Correl. distance = distance between detectors D1

BV: Correl. distance = distance of propagation D2?

Question:

System = 2 photons

Apparatus = mirrors + detectors

or

System = 2 photons + mirrors

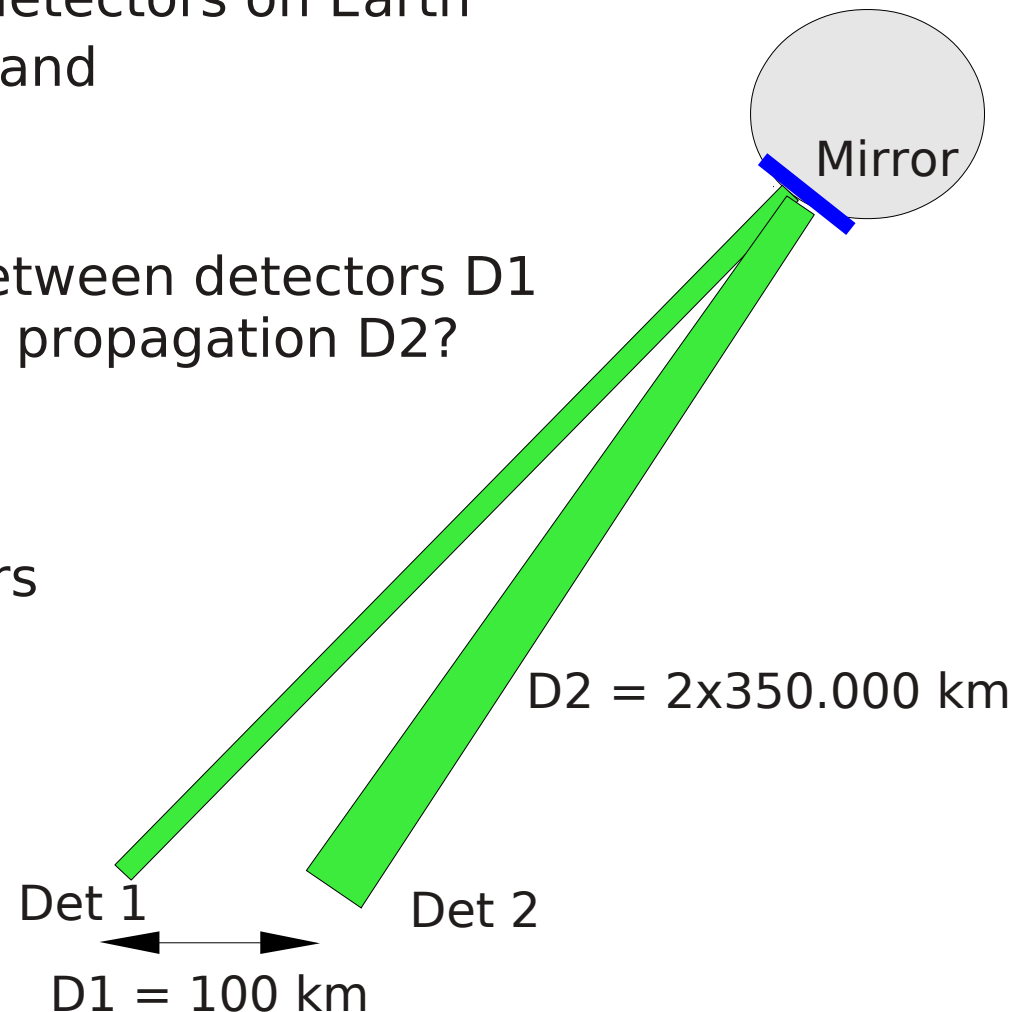
Apparatus = detectors

==>

Root of concept of measurement.

Strict QM: measurement = appearance of a number on a display

Naive view: measurement = system-apparatus interaction



# A fundamental question

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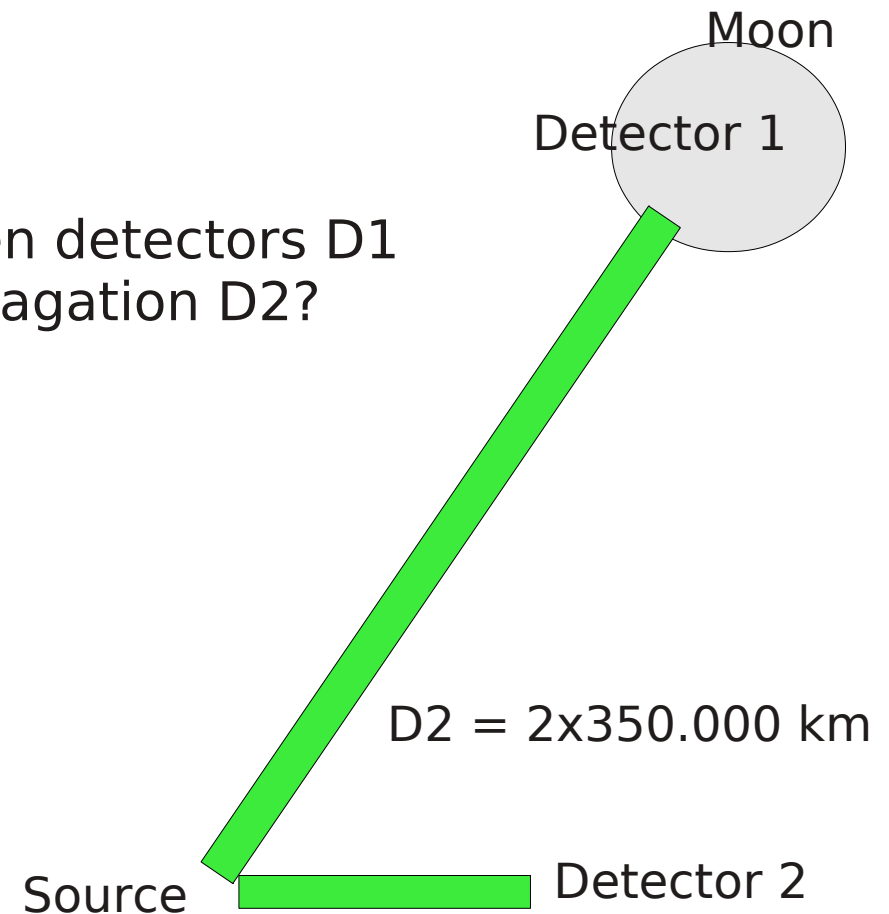
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# An Earth-Moon laser

Mirror deposited on the Moon by Apollo



- The Apache Point Observatory's 3.5 meter telescope
  - Southern NM (Sunspot)
  - 9,200 ft (2800 m) elevation
  - Great "seeing": 1 arcsec

# Toward a real implementation



**D O C U M E N T**

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document title/ titre du document

## ***DIRECTORATE OF HUMAN SPACEFLIGHT***

### ***ESA FIRST LUNAR LANDER: REQUEST FOR INFORMATION***

See also: Science from the Moon (Burns et al)  
arXiv:0909.1509

# Prospects for a Lunar Base

- Prerequisite to establish a permanent Lunar base: **Water**

Permanent at the frozen polar regions (T= 100 K) ?

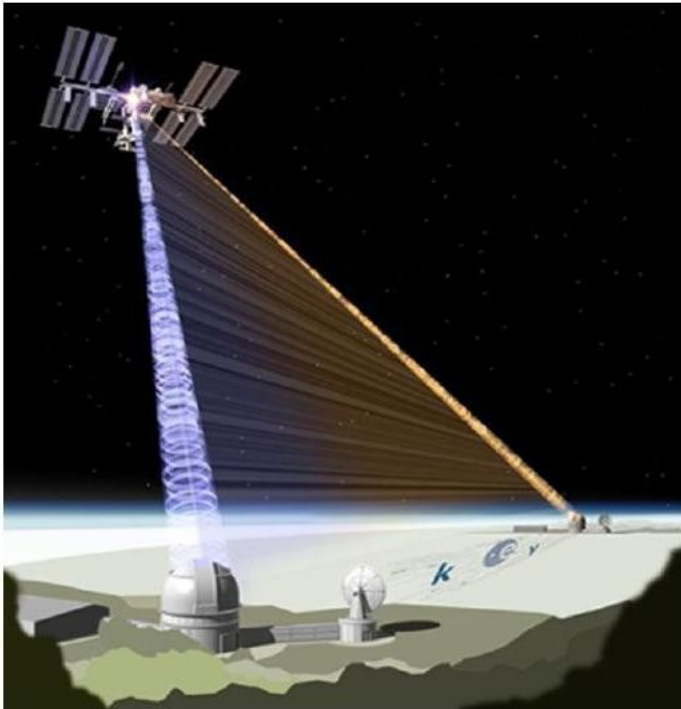
Natural sources:

- Bombardement by comets
  - H+ in stellar wind + O in lunar rocks --> H<sub>2</sub>O ==> 10<sup>7-8</sup> tons
  - Check underway after NASA/LCROSS crash on the Moon (12 Oct)
- Plans to establish a permanent Lunar base:
    - Under study: European Lunar Lander (ESA, Astrium/DLR)
    - Preparation: European, NASA « Lunar Science Institutes »
    - 23 October 2009: ESA+EU Ministerial Conference in Prague to establish « a policy in the field of exploration of our solar system, going back to the Moon ».



# Other possibilities

- ISS: projet Space-QUEST (Ursin et al. 2008)



Problems:

- less room than on Moon
- distance = 400 km instead of 400.000 km
- duration of individual experiments:  
a few minutes/hour
- 400 km experiments will certainly become possible on Earth thanks to progress in fiber optics

- Planet Mars (Kaltenbaek 2003): very futuristic
- LISA? (5 million km) See poster by Acef et al. for LISA lasers
- **Transfer correlated quantum states in free boxes at the edge of the Solar System:**  
no technological possibility foreseen